

Measurement of correlation between polarization of annihilation photons emitted in e^+e^- system to detect entanglement at MeV range



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Introduction and Motivation

Quantum electrodynamics predicts that photons originating from the decays of e^+e^- annihilations are entangled and have mutually orthogonal polarization [1]. Since the polarization of the photons is orthogonal to each other, correlation can occur in subsequent interactions. Compton scattering of photons can be used as a polarization analyser to measure such correlations [2]. To measure the correlation between the scattered photon due to entanglement, the two photons must be detected before and after the scattering [3].

Methodology

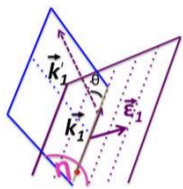
Klein-Nishina differential cross section

$$\frac{d\sigma(E, \theta, \eta)}{d\Omega} = \frac{r_0^2}{2} \left(\frac{E'}{E}\right)^2 \left(\frac{E'}{E} + \frac{E}{E'} - 2 \sin^2 \theta \cos^2 \eta\right)$$

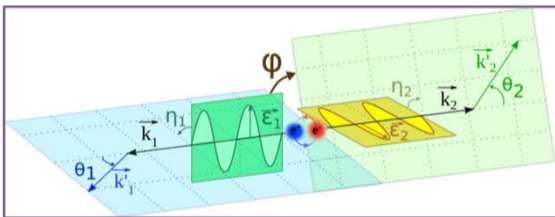
$$E'(E, \theta) = \frac{E}{1 + \frac{E}{m_e c^2} (1 - \cos \theta)}$$

- An incident photon is mostly scattered **perpendicular** to the polarization direction of the incident photon.
- Polarization of a photon can be defined as

$$\epsilon = \mathbf{k} \times \mathbf{k}'$$



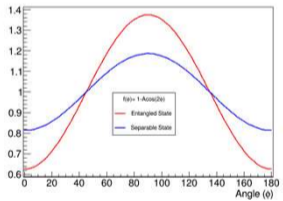
- For 2 annihilation photons, double Compton Scattering differential cross section



$$\frac{d^2\sigma_{double}}{d\Omega_1 d\Omega_2} = \frac{r_0^4}{16} \left[\frac{(1 - \cos \theta_1)^3 + 2}{(2 - \cos \theta_1)^3 (2 - \cos \theta_2)^3} - \frac{\sin^2 \theta_1 \sin^2 \theta_2}{(2 - \cos \theta_1)^2 (2 - \cos \theta_2)^2} \cos(2\phi) \right]$$

$$f(\theta, \phi) = 1 - A(\theta) \cos(2\phi)$$

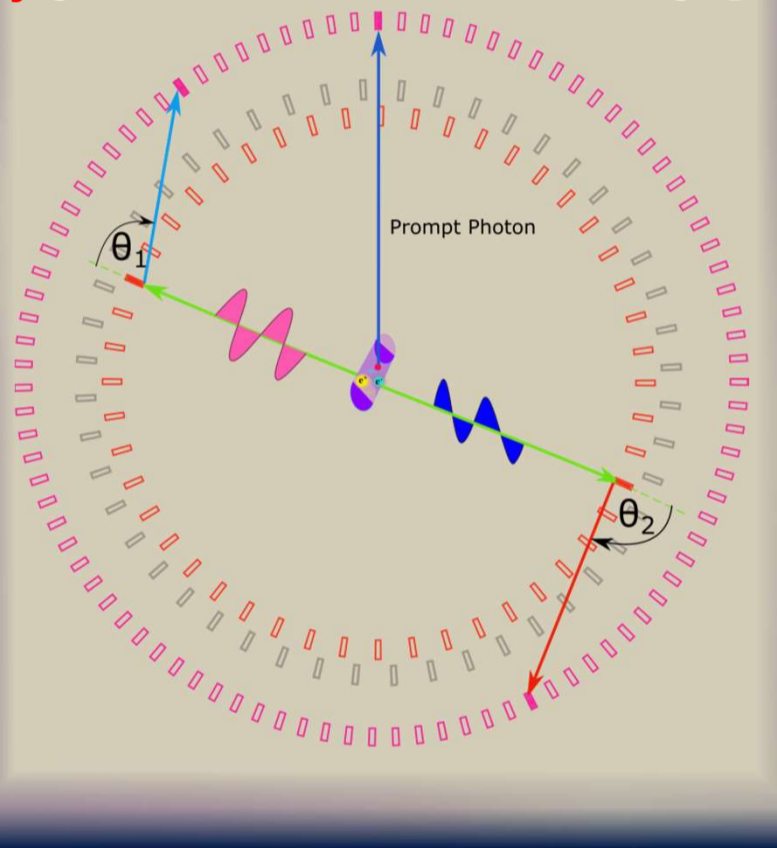
- $A = 0.48$ for entangled state
- $A = 0.23$ for separable state



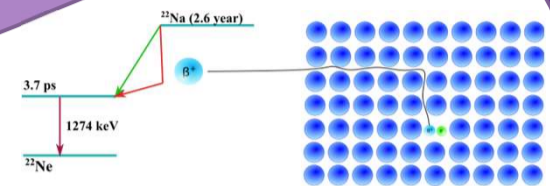
J-PET

- A potential detector to perform entanglement studies in MeV range [4,5,6].
- 192 plastic scintillators : 50 x 1.9 x 0.7 cm³
- 3 cylindrical layers : 42.50 cm, 46.75 cm and 57.5 cm.
- Angular Resolution ~ 1°

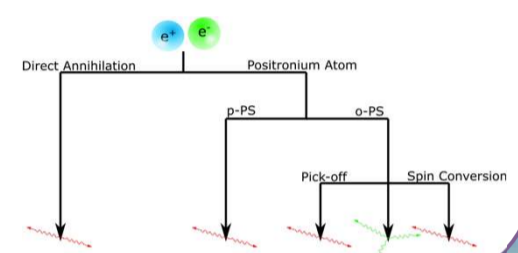
Jagiellonian Positron Emission Tomograph



Positronium formation



Positronium annihilation channels

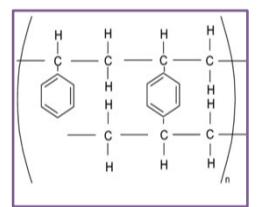


Experimental Details

Source : ²²Na (1 MBq)

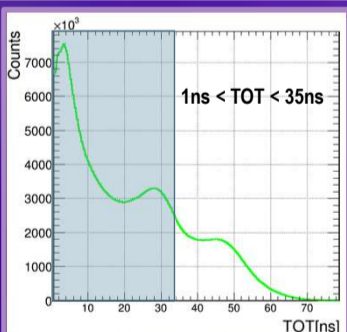
Chamber

Material : XAD-4

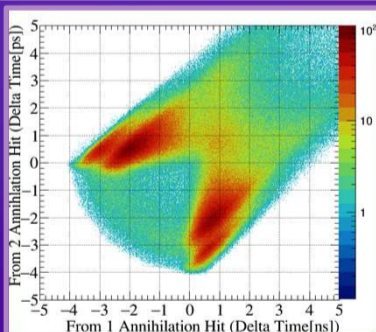


An experiment was performed using a plastic chamber by placing a source in its centre surrounded by the XAD-4 material. XAD-4 is a material with high porosity (~90% of empty volume)

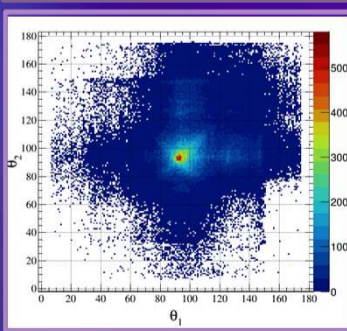
Preliminary Results



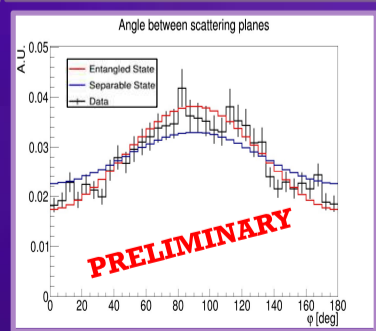
Time Over Threshold (TOT) as a measure of Energy Deposition



Scatter Test (S) = $\Delta t - d/c$
Assignment of the scatter hit to primary hit



Correlation between the scattering angles
 $(\theta_1 - 100)^2 + (\theta_2 - 100)^2 = 30^2$



Comparison between experimental data and theoretical predictions

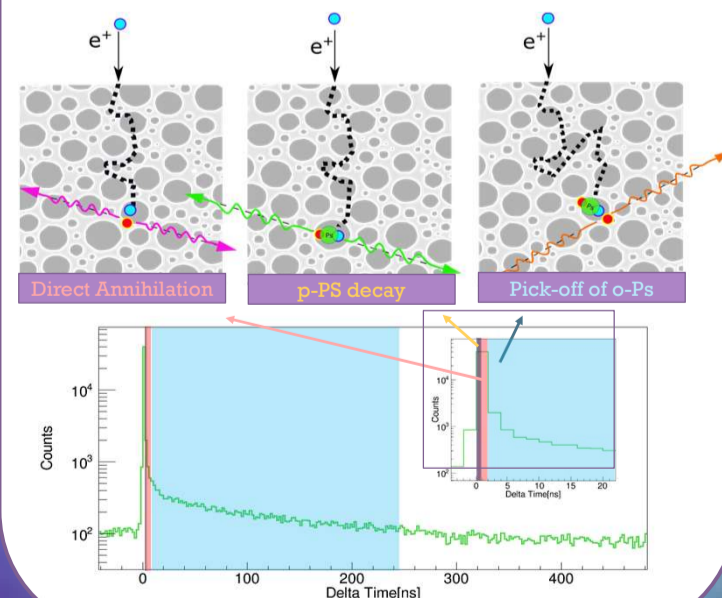
Summary

J-PET is a unique detector, which can be used to perform the measurement of the correlation of polarization of annihilation photons emitted in e^+e^- system in full phase space.

- It is theoretically predicted that the annihilation photons originating from e^+e^- system are entangled and their polarization directions are orthogonal to each other.
- Orthogonality in the polarization of photons leads to an enhanced correlation in the scattering plane of both photons.
- Theoretically, the maximum visibility of the correlation is at scattering angle of ~ 82°
- In this work, we present preliminary results for experimentally measured polarization correlation and compared the result with the theoretical predictions.

Future Prospective

- Use the positronium lifetime spectra to distinguish the influence of different positronium annihilation channels on the polarization correlation of emitted back-to-back photons.



References

[1] Snyder, H. S., Pasternack, S. & Hornbostel, J Phys. Rev.73, 440 (1948)
 [2] O. Klein, Y. Nishina, Z. Physik 52, 853 (1929)
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Acknowledgement

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